

A 3D ball-and-stick model of a graphene lattice structure, showing a hexagonal arrangement of atoms (represented by light blue spheres) connected by bonds (represented by light yellow rods). The structure is shown in a perspective view, with a central layer in focus and other layers visible in the background, creating a sense of depth.

Graphene

a new electronic material

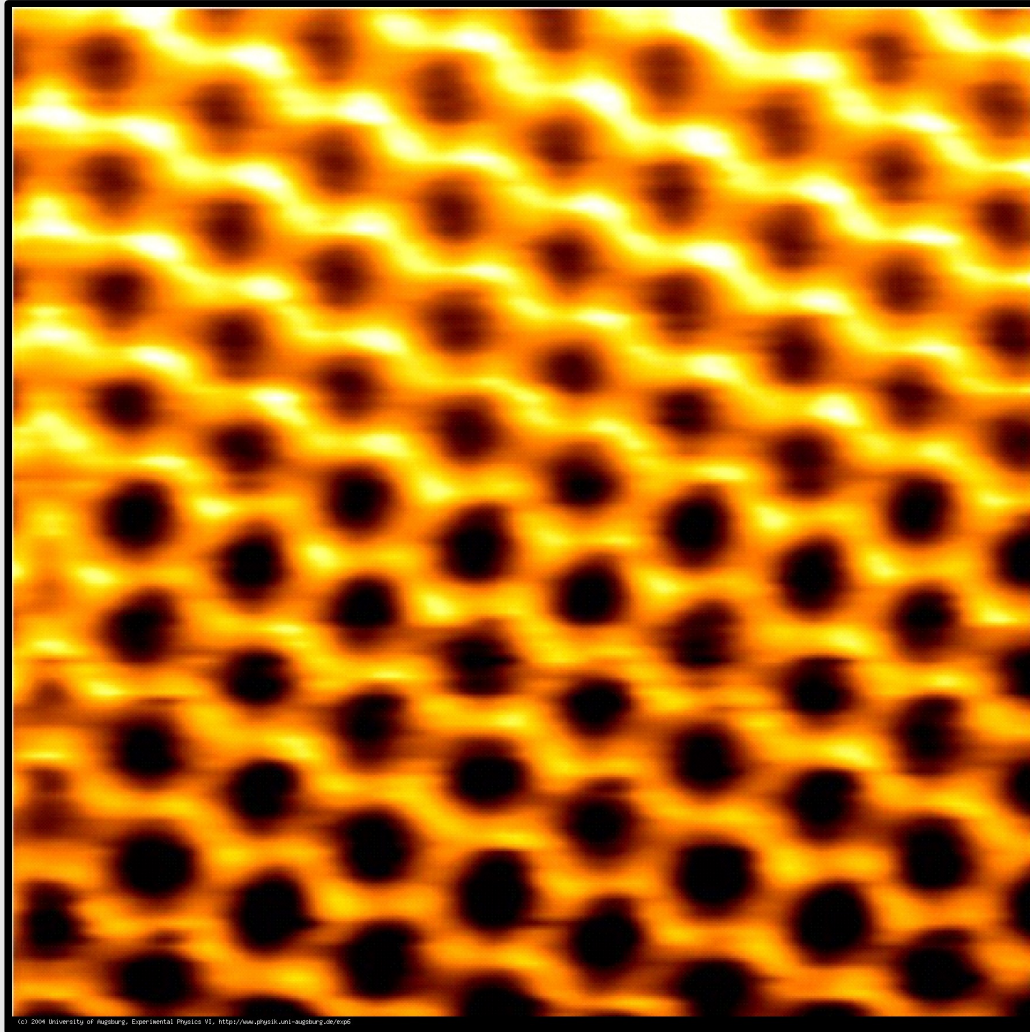
Anton Lopatin
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08.06.2007

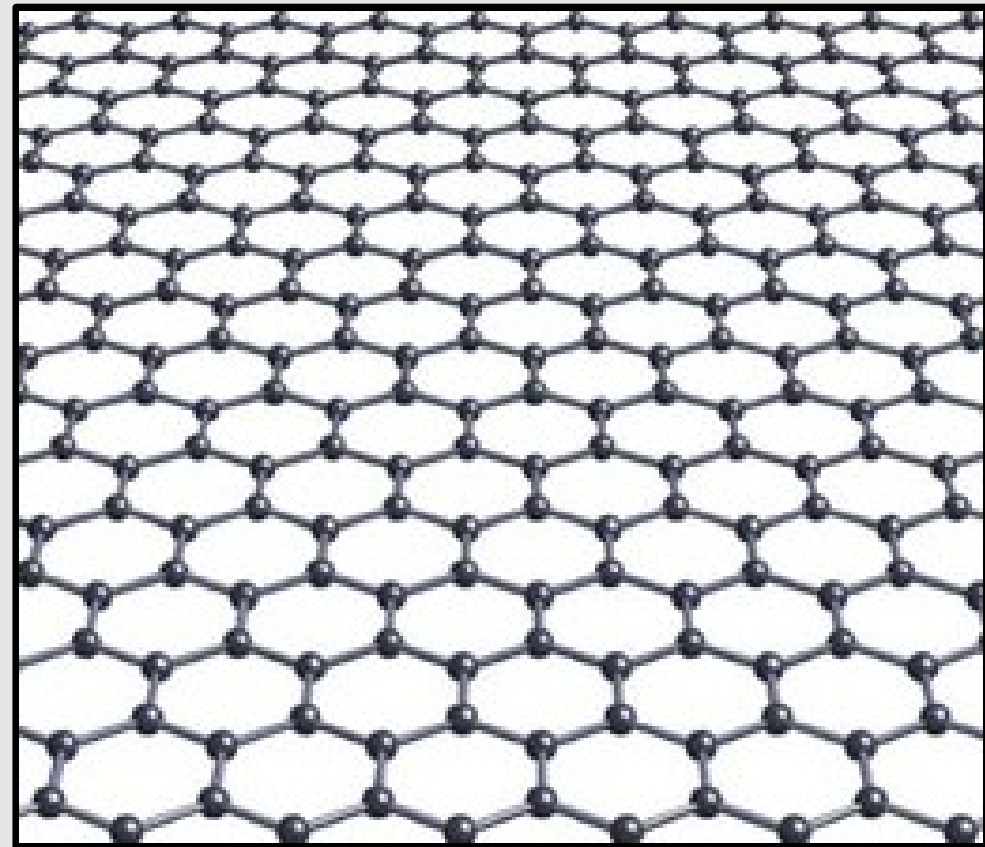
Overview / Roadmap

- Introduction
- Preparation of Graphene
- Atomic / Electronic Structure
- Description as Dirac Fermions
- Anomalous Quantum Hall Effect
- Tunneling of Chiral Particles
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- Conclusions

Graphene: a carbon modification



AFM image of graphite surface, $2 \times 2 \text{ nm}^2$
(Exp. Physics VI, Uni Augsburg)

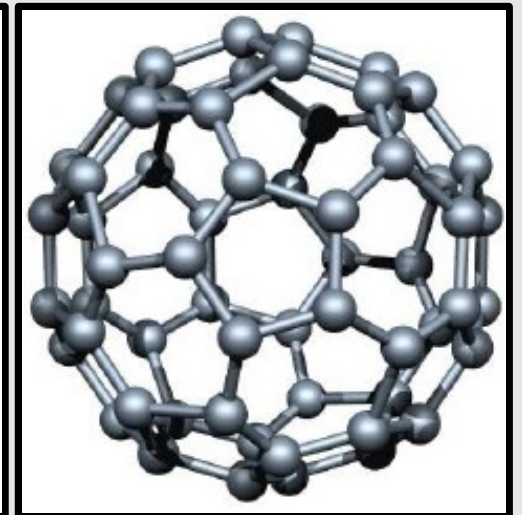
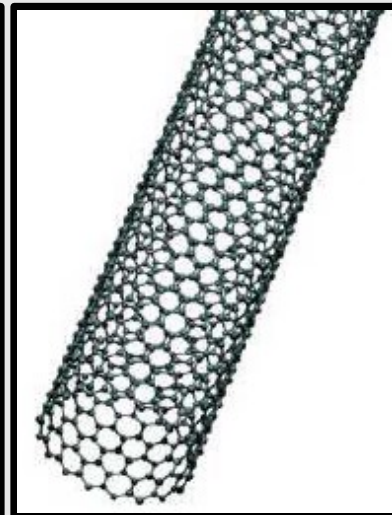
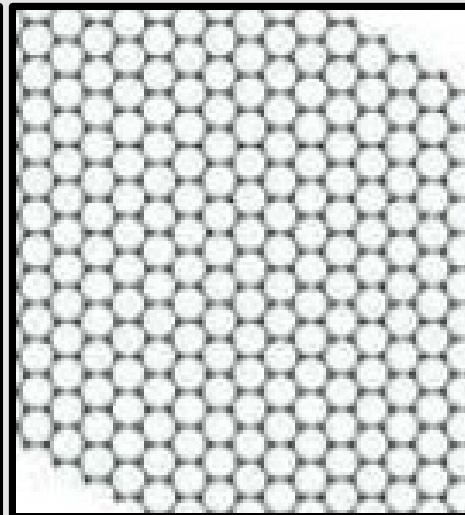
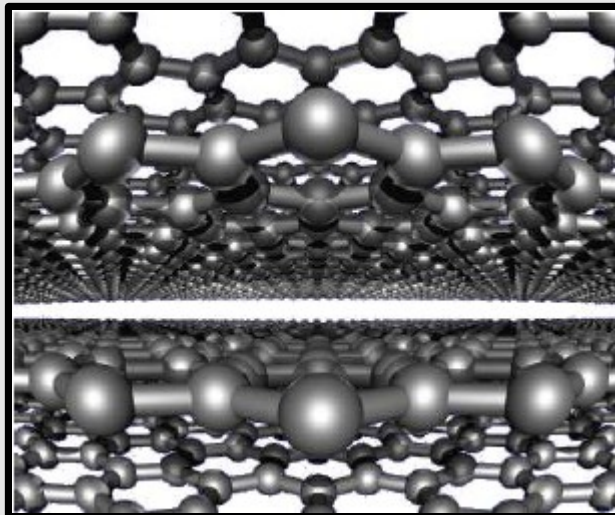
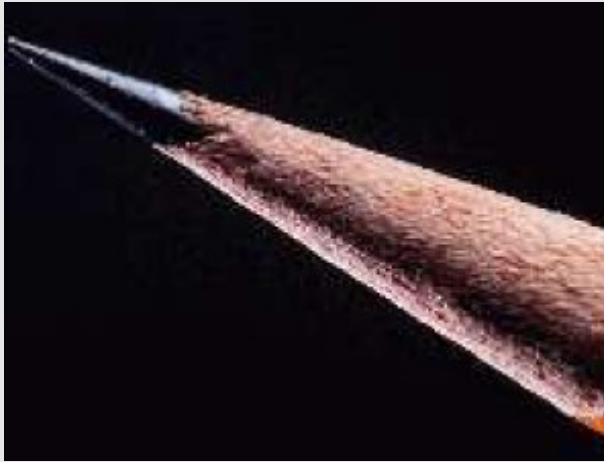


Planar, hexagonal structure of graphene

Introduction

Graphene in many dimensions:

- 3D in graphite crystals
- 2D in a single layer
- 1D in nanotubes
- 0D in fullerenes



Preparation of Graphene



Top – Down Approach:
Micromechanical cleavage

Bottom – Up Approach:
Growing Graphene on SiC



Top – Down Approach

(after Novoselov et al., Science 306, 666 (2004))

„Micromechanical cleavage“

Recipe:

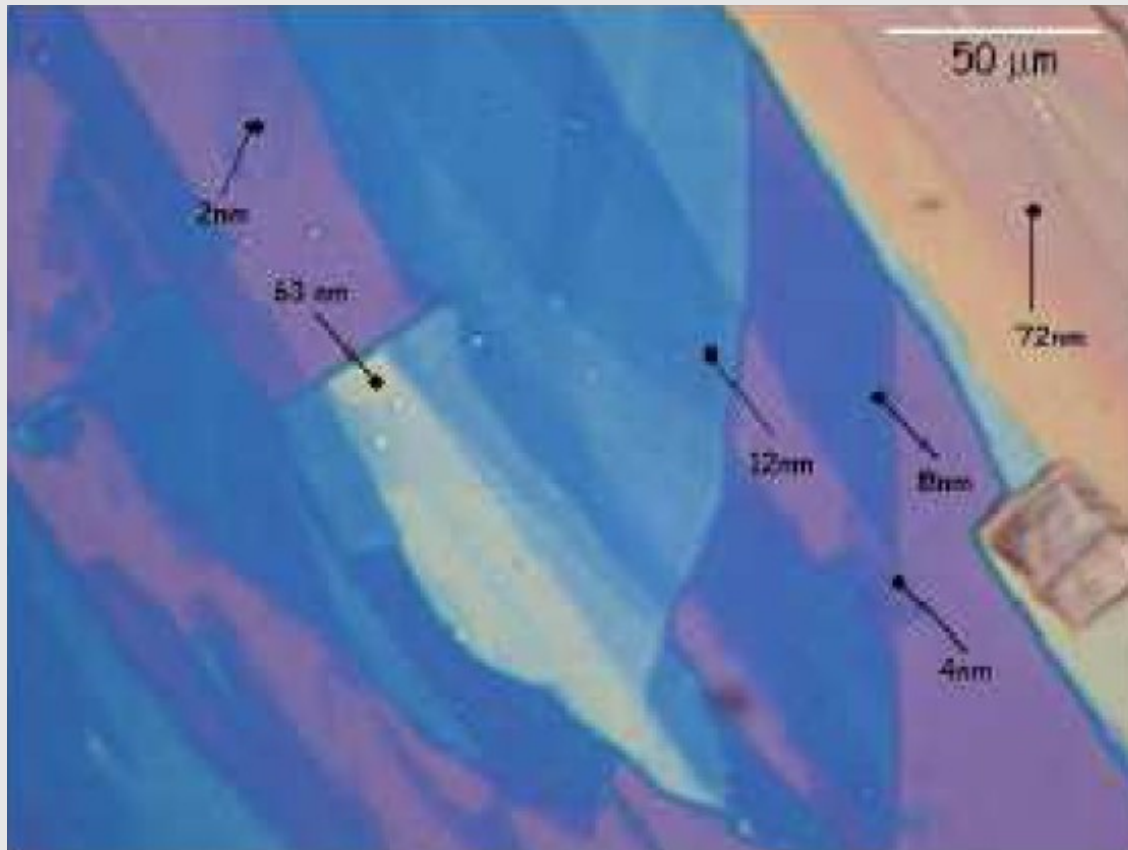
1. 1mm **highly-oriented pyrolytic graphite** (HOPG)
2. **dry etching**: 5 μ m
3. photoresist on glass surface, **baking** layer into it
4. **peel of** layers using scotch tape
5. **release** thin flake left on glass in acetone
6. „**wash**“ flake on wafer
7. **ultrasound cleaning** in propanol: only thin flakes stick to SiO₂



Top – Down Approach

(after Novoselov et al., Science 306, 666 (2004))

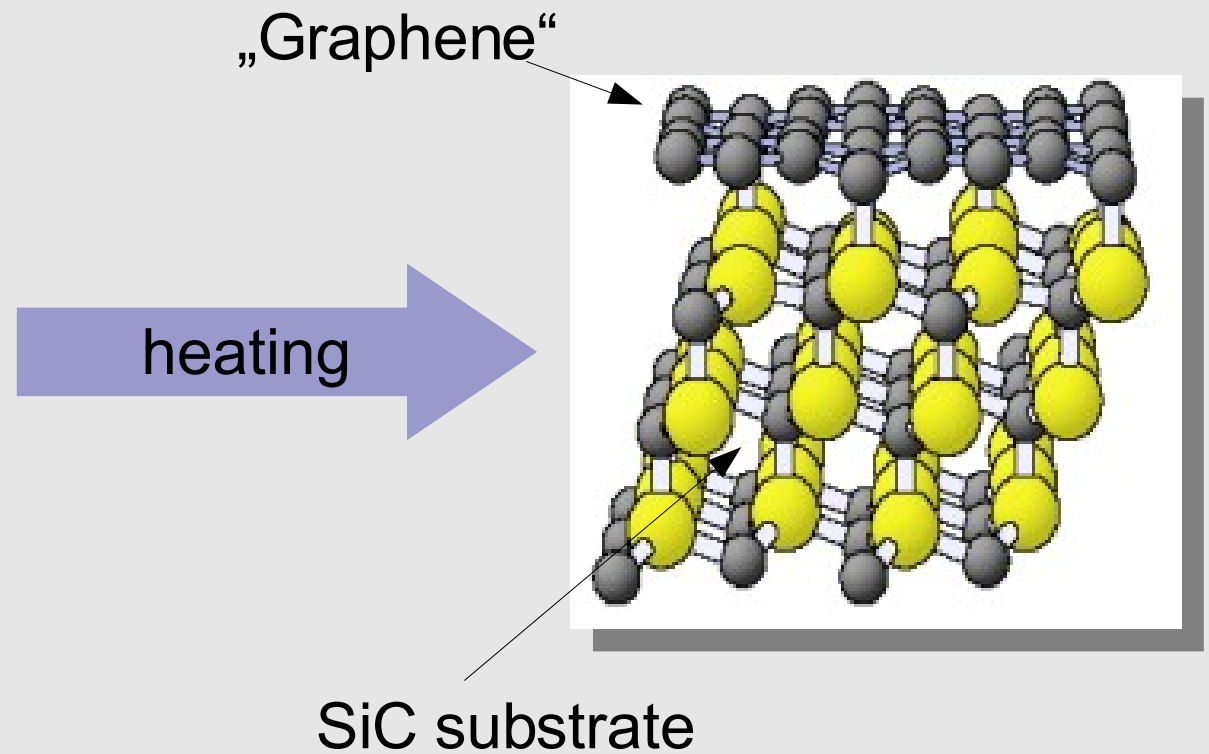
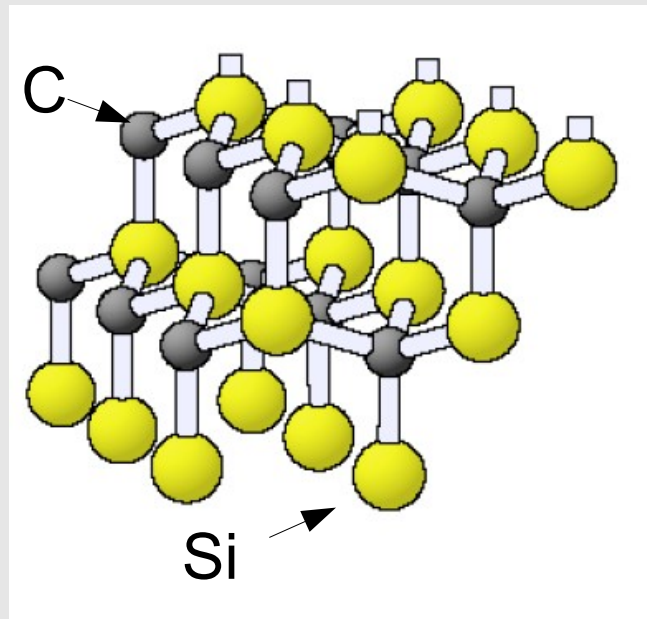
Final step: **selection process** finding thin layers using optical microscope, scanning electron micrographs, AFM



Wafer with graphene flakes, optical microscope

Bottom-Up Approach

Growing Graphene on SiC

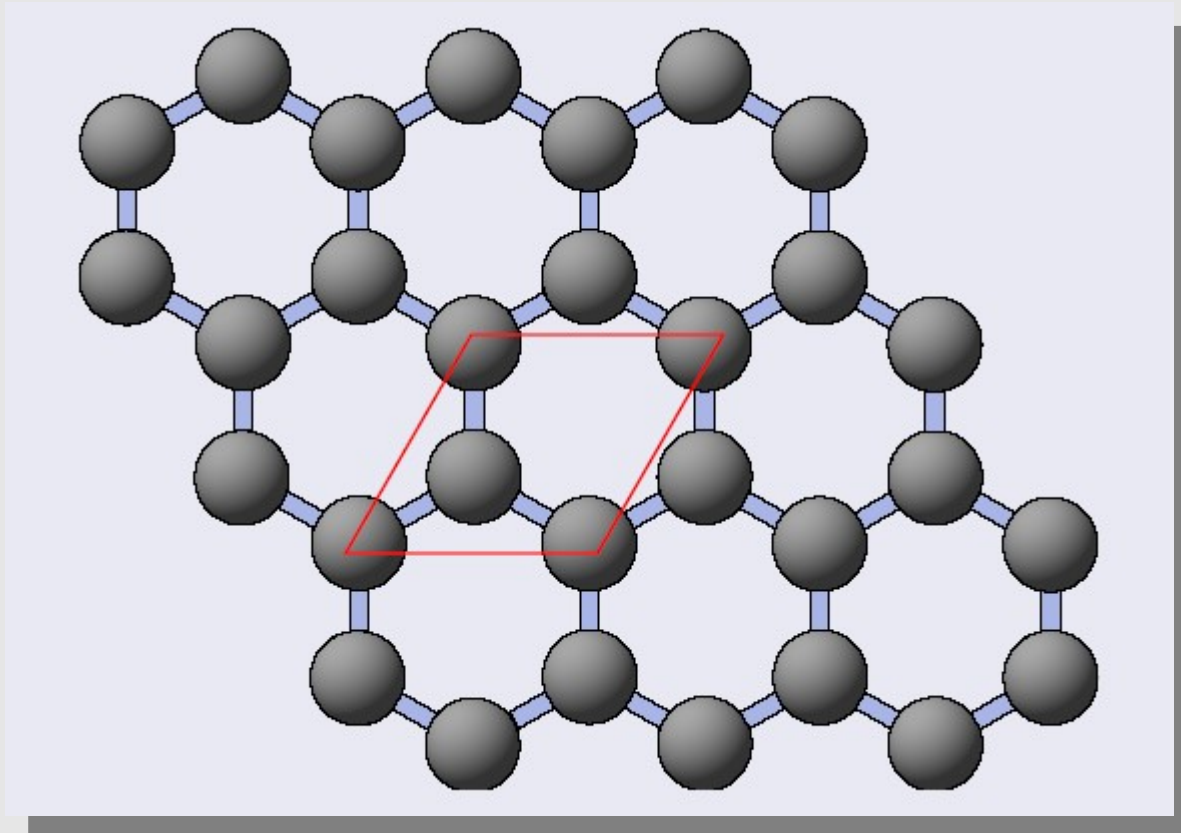


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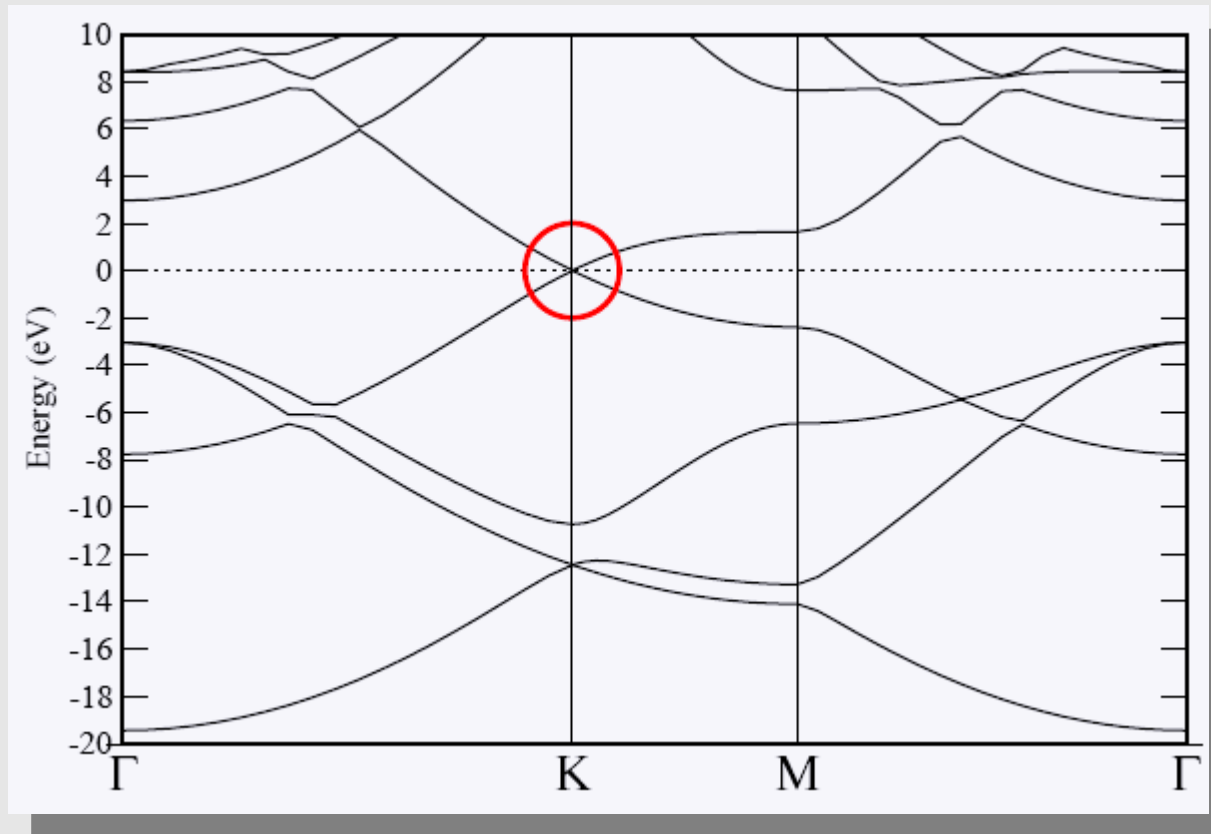
Atomic Structure

- sp^2 hybridization \Rightarrow planar, hexagonal lattice



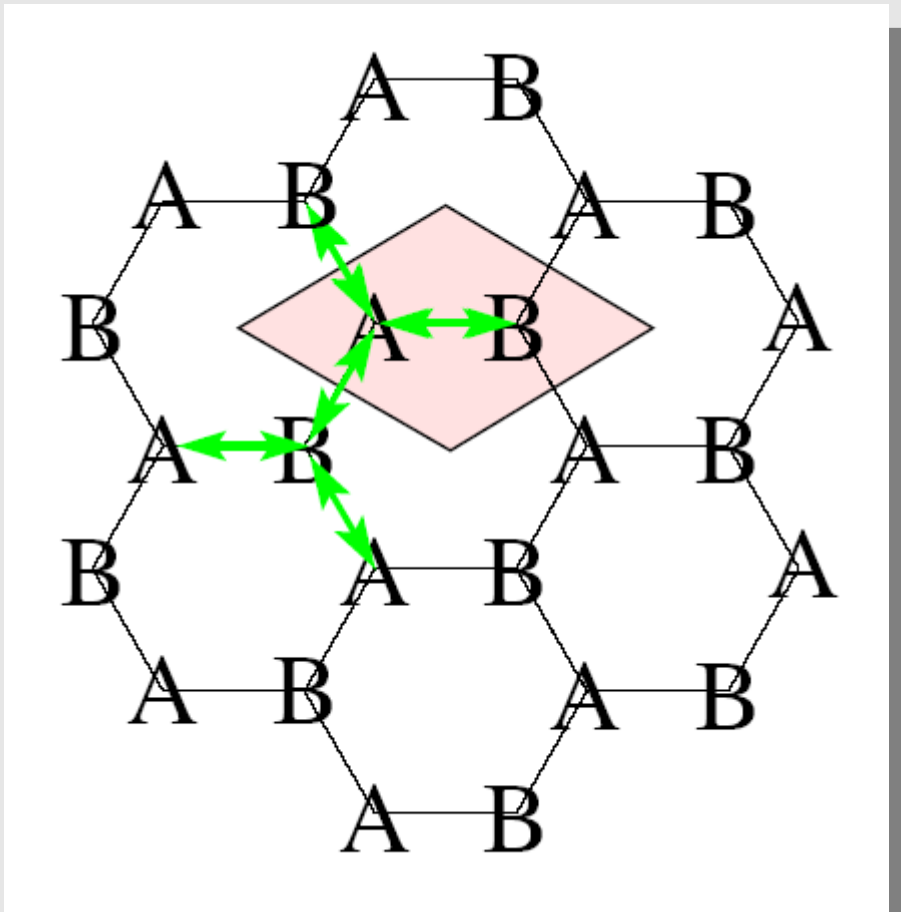
- $a = 2.45 \text{ \AA}$
- 2 carbon atoms per unit cell

Electronic Bandstructure

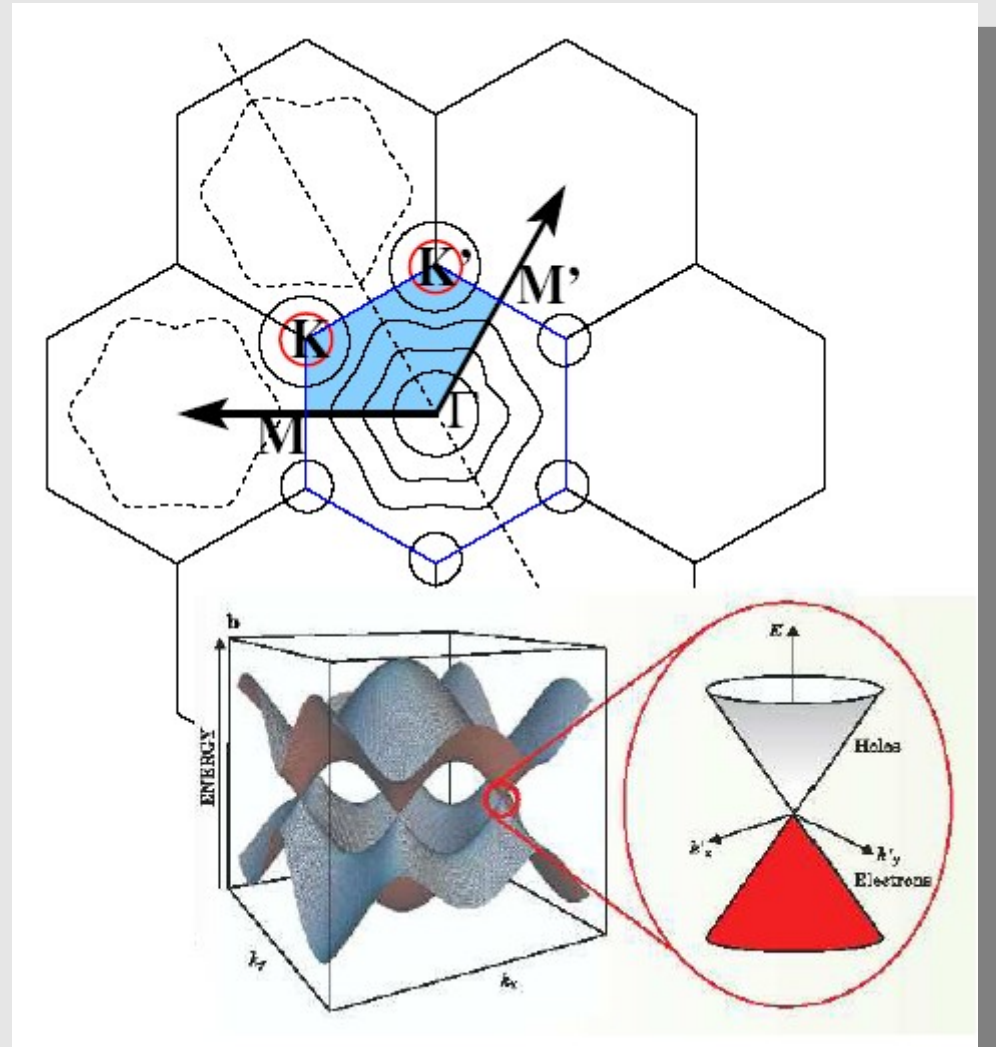


- gapless semiconductor \Leftrightarrow semi-metal
- linear dispersion relation at conic point

Bipartite lattice

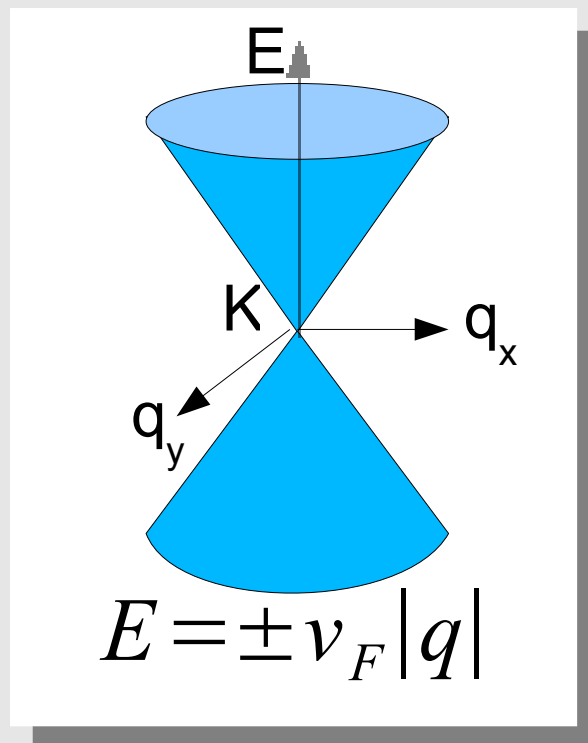


real space



momentum space

massless 2D Dirac Fermions



$$H_K = \begin{pmatrix} 0 & v_F(q_x - iq_y) \\ v_F(q_x + iq_y) & 0 \end{pmatrix}$$

- $q = K - k$
- 2x2 structure from 2 site unit cell => pseudo spin

„light cone“ with $v_F = 10^6$ m/s

Pseudo spin

$$H_K = \begin{pmatrix} 0 & v_F(q_x - iq_y) \\ v_F(q_x + iq_y) & 0 \end{pmatrix} = v_F \begin{pmatrix} \sigma_x & \sigma_y \end{pmatrix} \begin{pmatrix} q_x \\ q_y \end{pmatrix}$$

- Pseudo spin commutes with $H_K \Rightarrow$ is conserved
- Pseudo spin is projected on momentum
 - σ parallel $q \Leftrightarrow$ electron
 - σ antiparallel $q \Leftrightarrow$ hole

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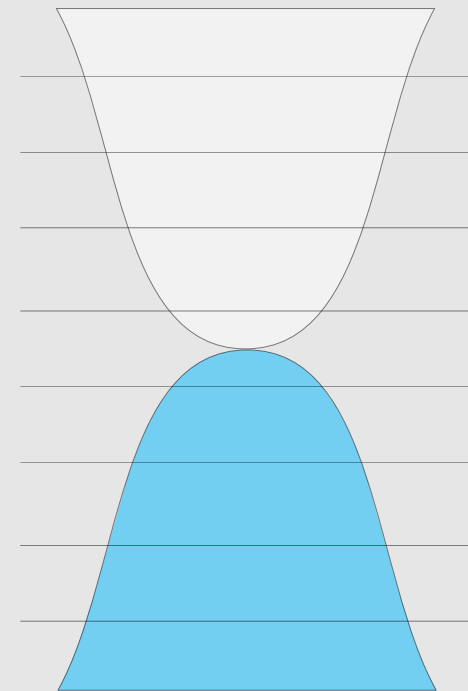
Anomalous QHE: setup

Landau quantisation

- from Schrödinger's Eq. (non relativistic):

$$E_n = \pm \hbar \omega_c \left(n + \frac{1}{2} \right)$$

↑
electron/hole
states



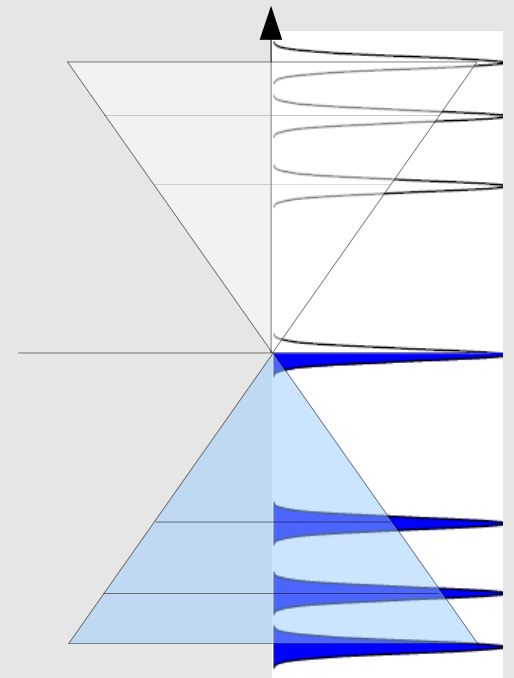
Landau quantisation (II)

- from Dirac Eq. (relativistic, massless):

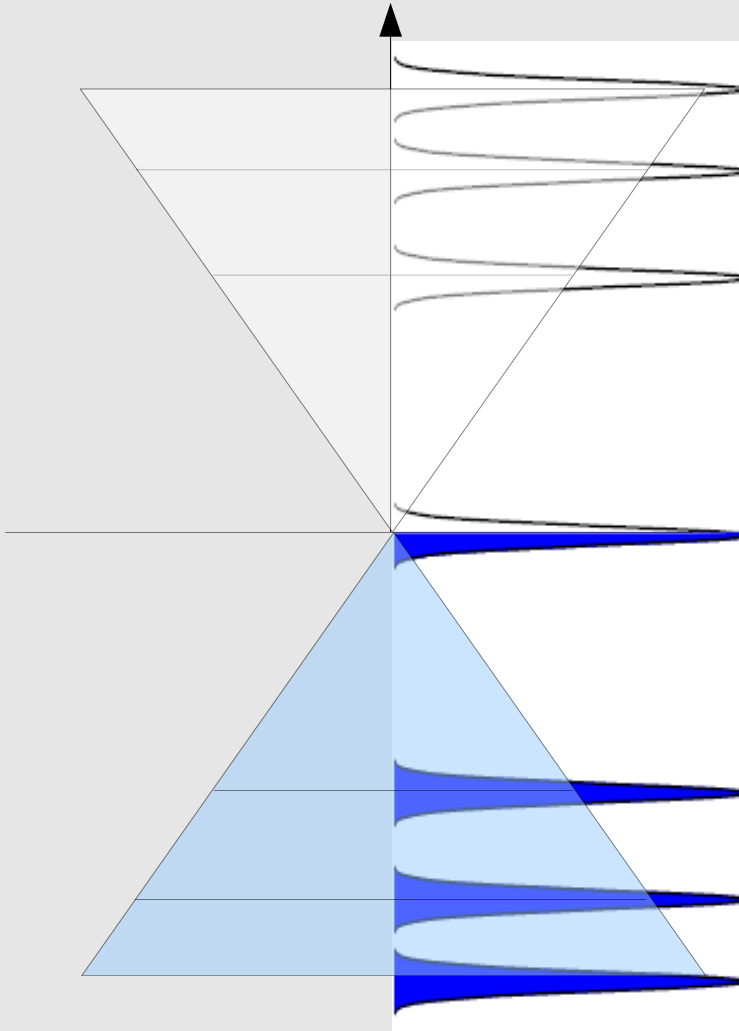
$$E_n = \pm \sqrt{2|e|B\hbar v_F^2 \left(n + \frac{1}{2} \pm \frac{1}{2} \right)}$$

↑
electron/hole
states

↑
pseudo spin



Landau quantization (III)

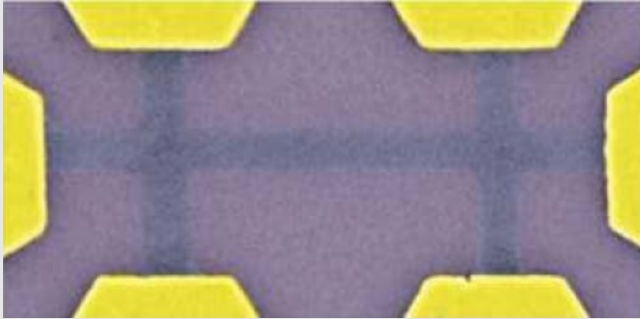


- There is an zero energy level! It doesn't move!
- Landau levels degeneracy:
 - $E = 0$: $2x$
 - $E > 0$ or < 0 : $4x$

Understanding QHE: σ_{xx}

Understanding QHE: σ_{xy}

Anomalous QHE in graphene



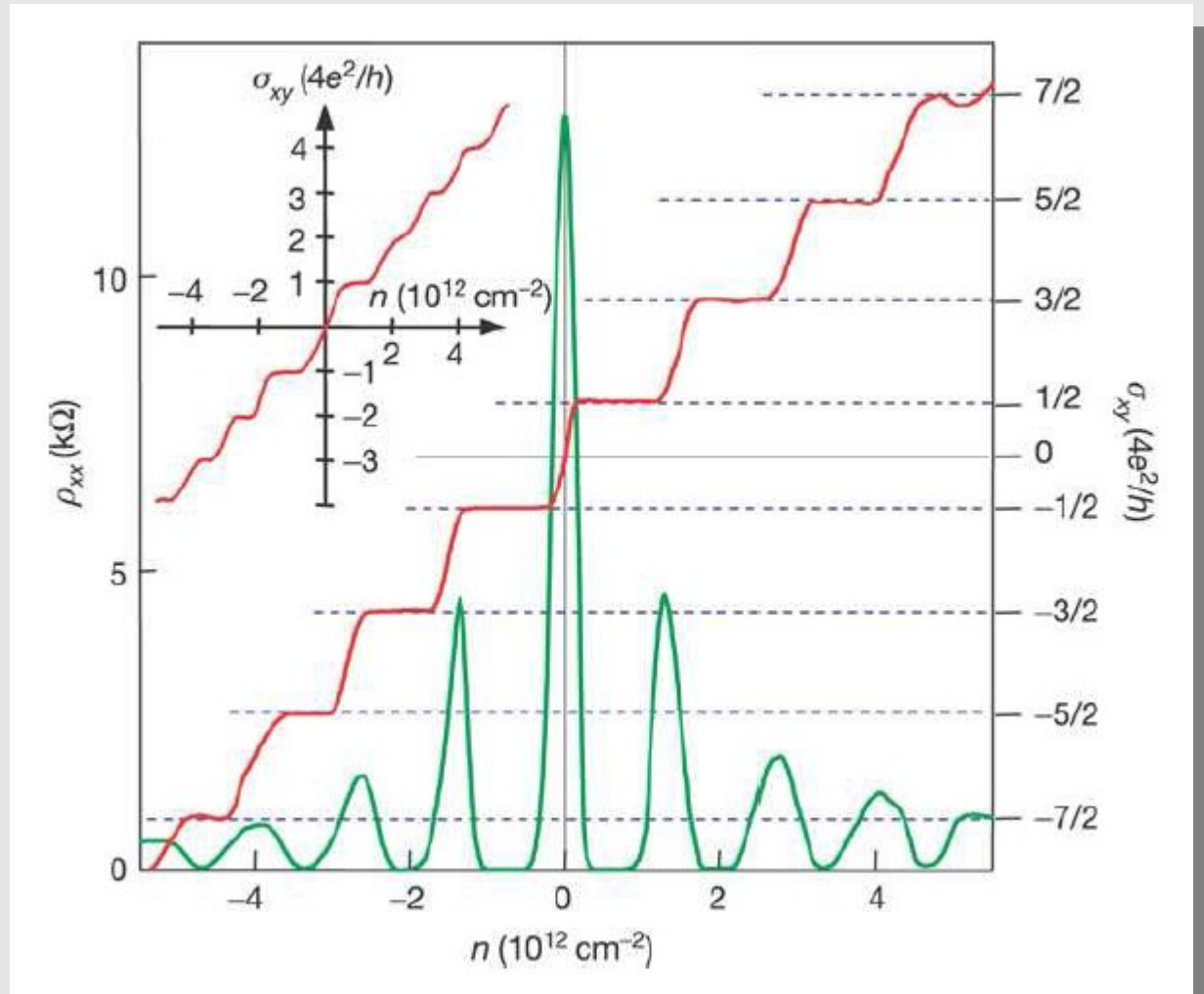
Hall bar, SEM false colors (L=200nm)

QHE in graphene

$$\sigma_{xy} = 4 \left(\frac{e^2}{h} \right) \left(n \pm \frac{1}{2} \right)$$

normal QHE

$$\sigma_{xy} = \left(\frac{e^2}{h} \right) n$$



(Novoselov et al., Nature 2005)

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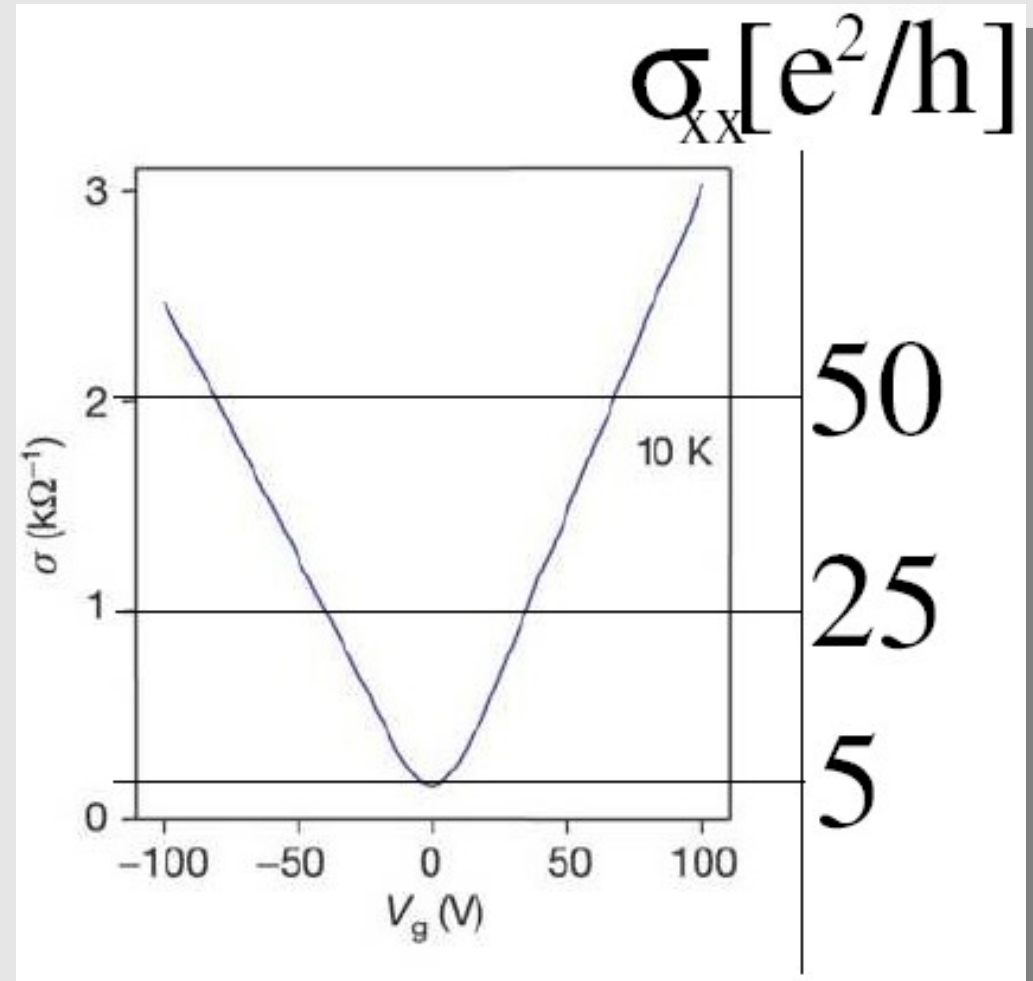
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Tunneling of Chiral Particles

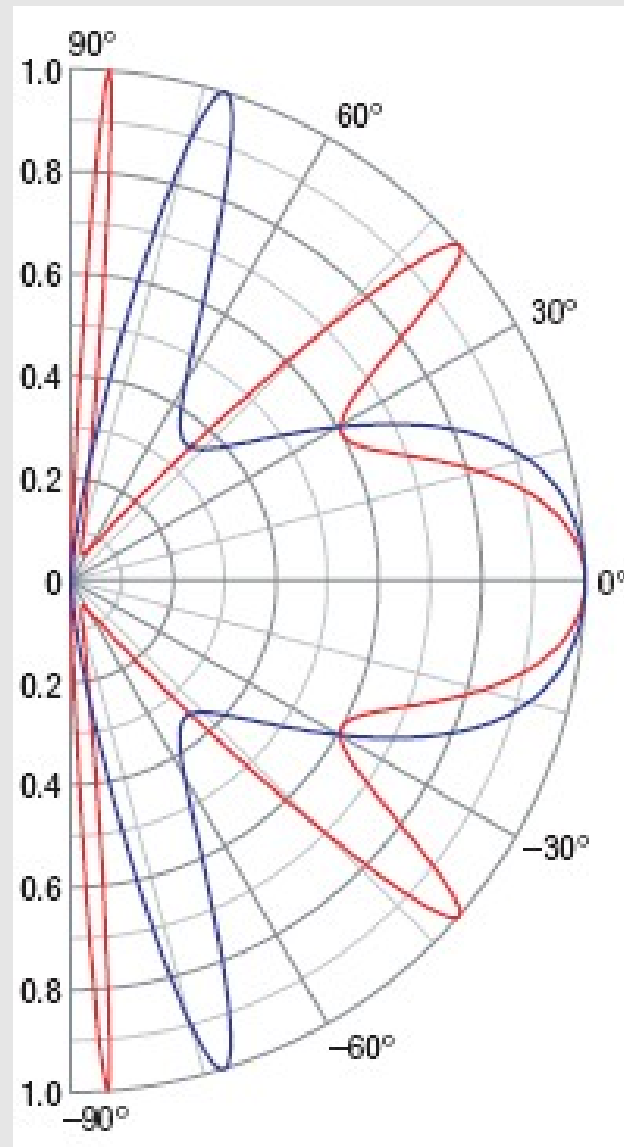
Motivation:

1D and 2D electron systems should crystallize at low temp. => there should be no conductivity

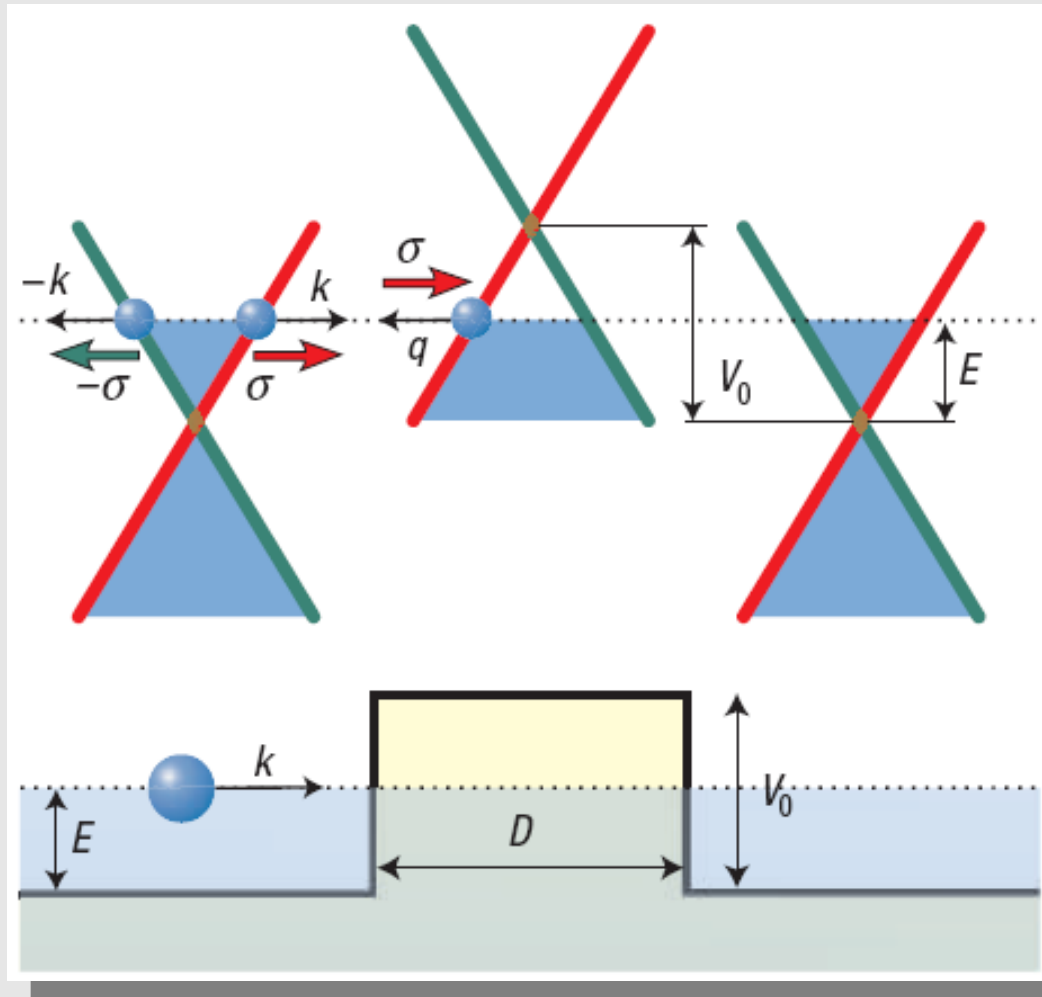
In graphene, this is not observed!!!



Forbidden Backscattering



Tunneling of Chiral Particles



electronic states outside the barrier
meet holelike states inside the barrier

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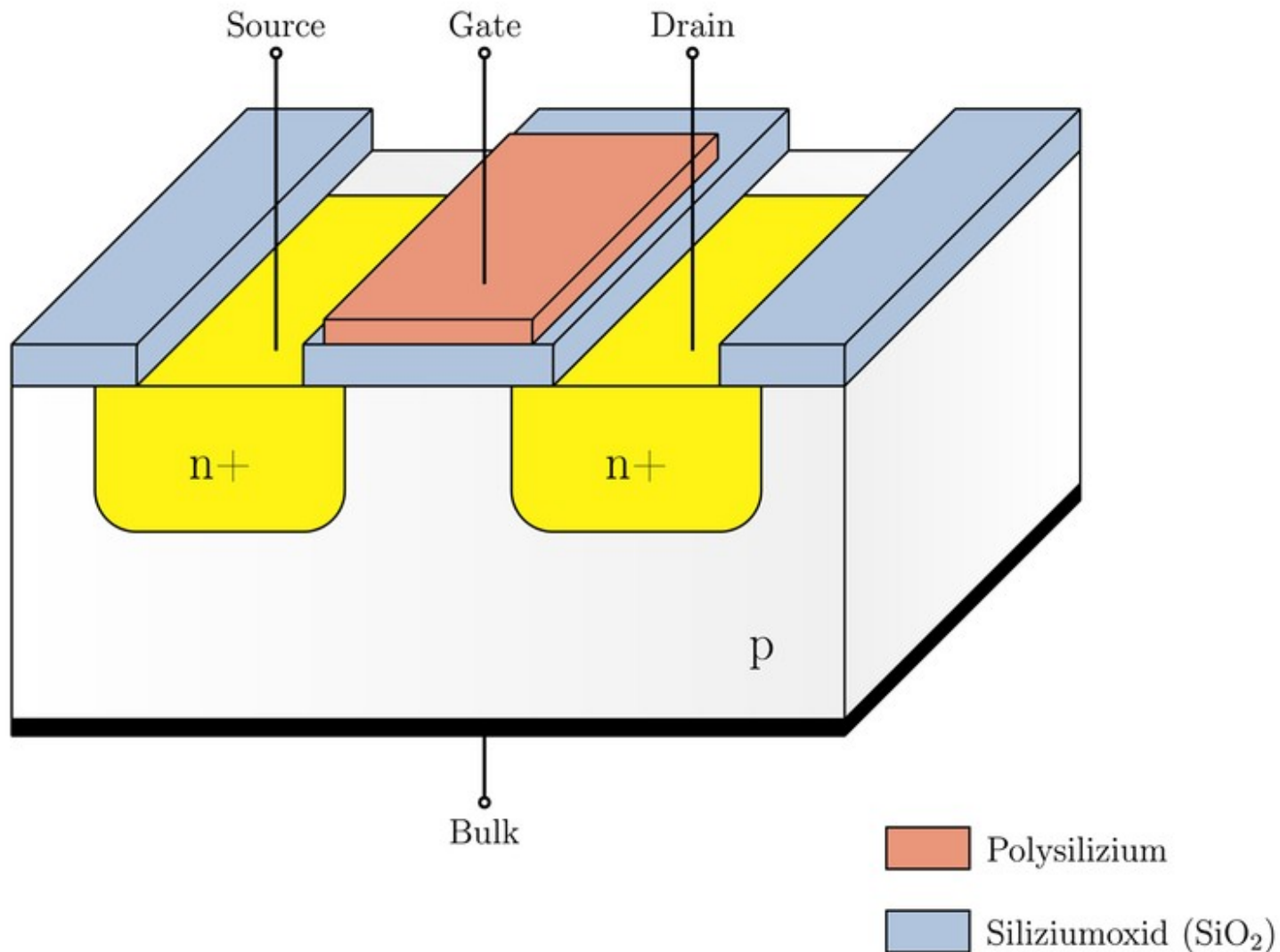
Graphene Devices: Electron mobility

- Graphene: 20.000 cm²/Vs to 50.000 cm²/Vs (only limited by defects, stable btw. 10 to 100K)

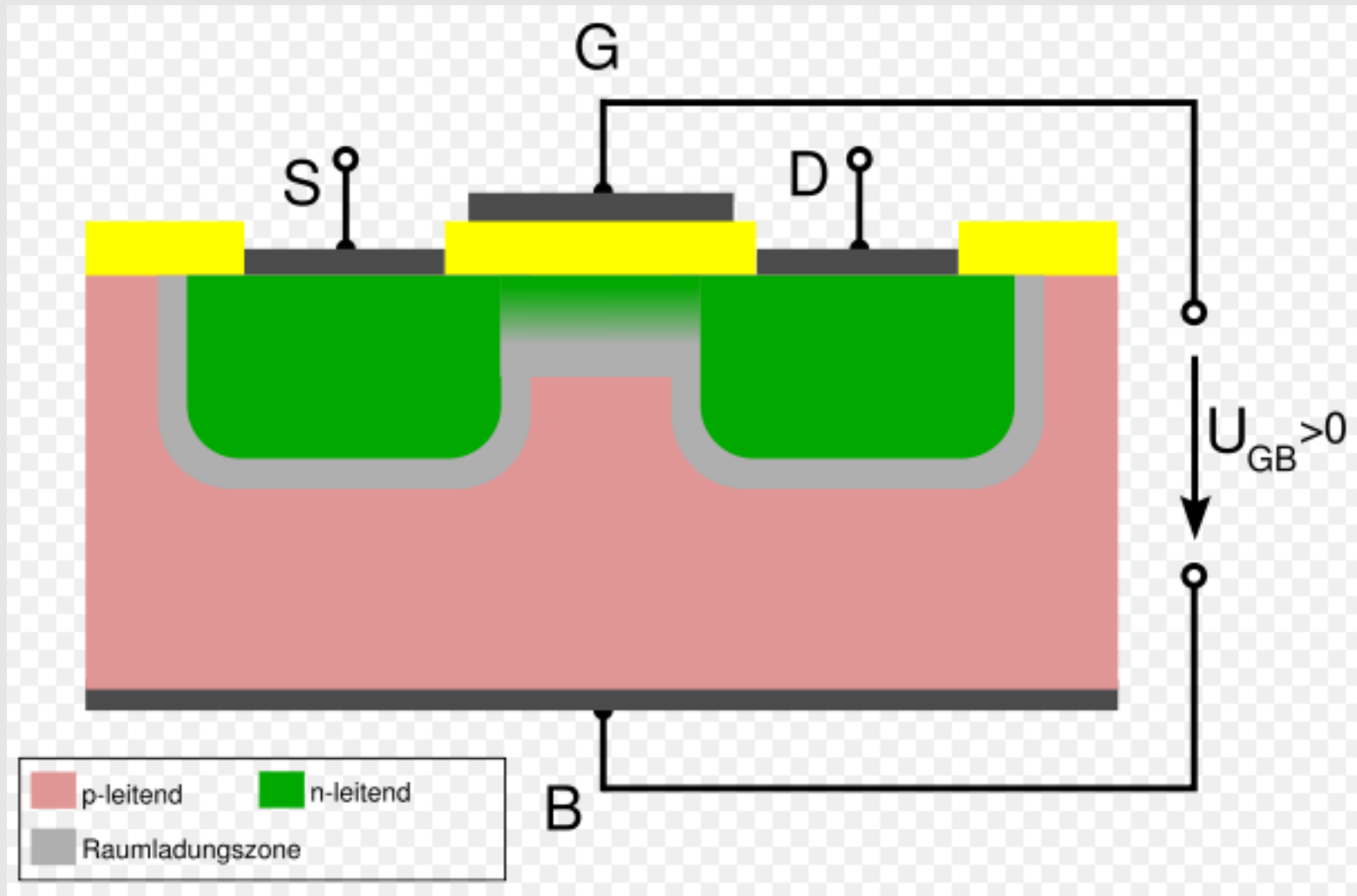
Current technologies:

- Silicon: 10.000 cm²/Vs (max)
- InSb (indium antimonide): 30,000 cm²/Vs at 295K (Intel, Qinetq, 2005)

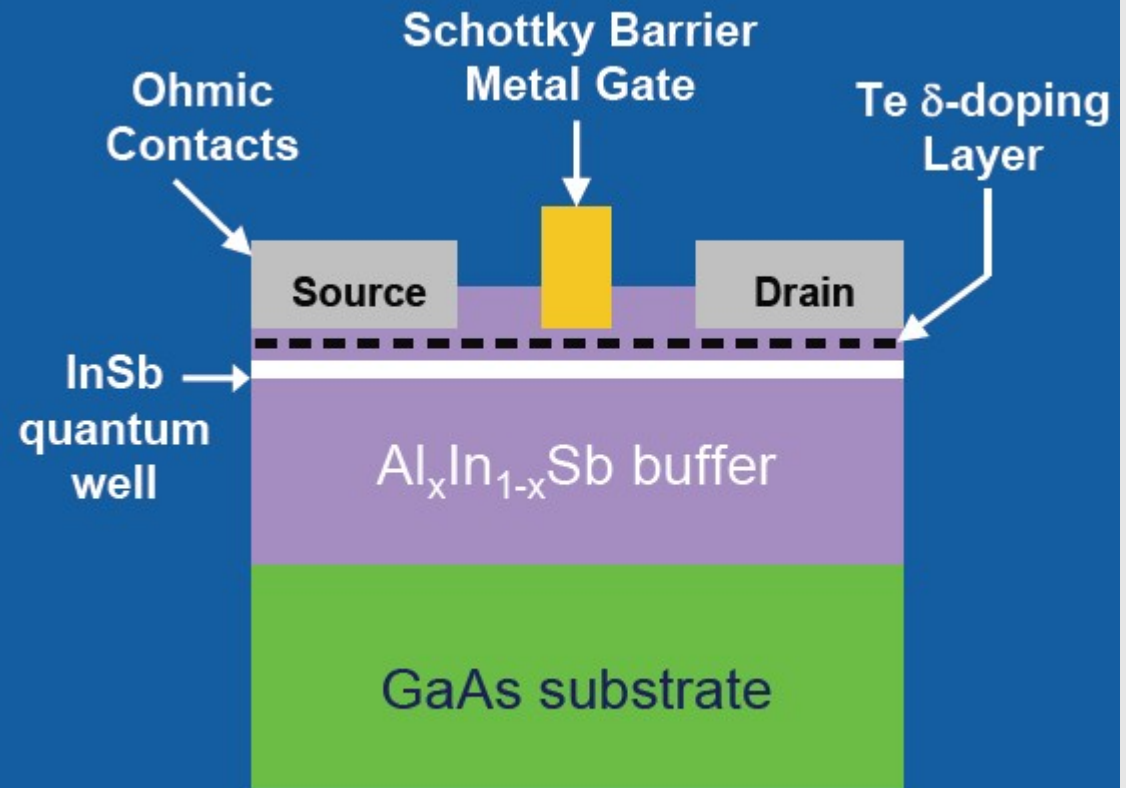
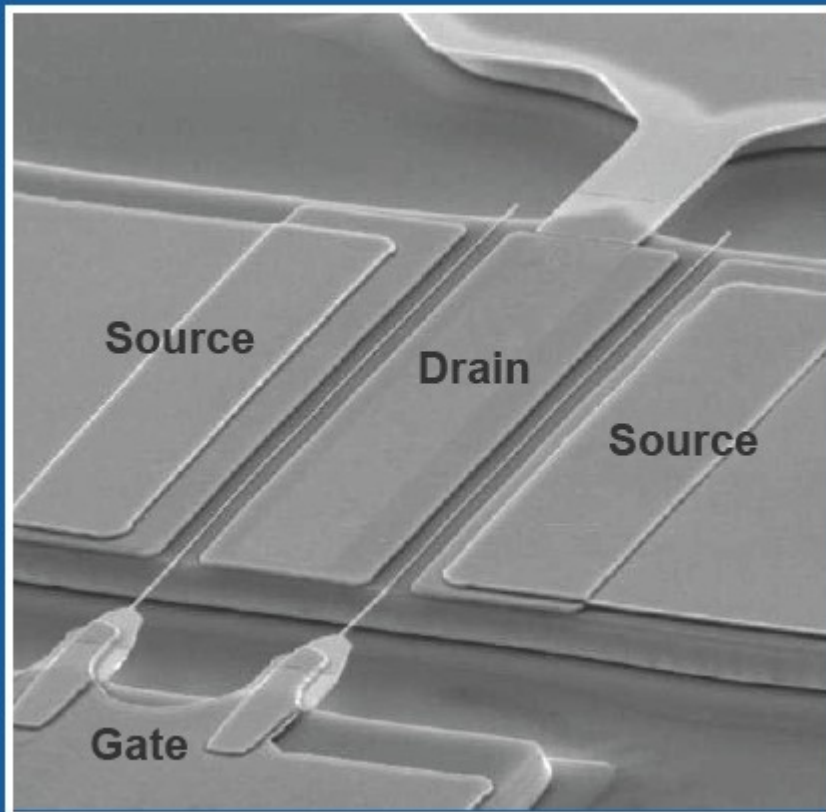
Classical FETs: n-MOSFET



n-MOSFET with channel



InSb quantum well transistors



(Intel , 3rd Asian Academic Forum, Nov. 2006)

Graphene FETs: simple design

- direct application: Gas sensor

Conclusions & Outlook

- unexpected bridge btw. condensed matter & QFT
- possibility to study 2D massless Dirac fermions in a bench-top setup
- (anomalous QHE, absence of Anderson localisation)
- Carbon transistors, with ballistic transport
- even more possibilities with bilayer graphene!

any questions?

THE END

Thank you for your attention. Have a nice day.