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## Efficient Algorithms and Datastructures II

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### Aufgabe 1 (10 Punkte)

In the maximum directed cut problem, we are given a directed graph  $G = (V, A)$ , and non-negative weights  $w_{ij} \geq 0, \forall (i, j) \in A$ . The goal is to partition  $V$  into 2 parts  $U$  and  $W$  so as to maximize the total weights of the arcs going from  $U$  to  $W$ . (we say that  $(i, j)$  goes from  $U$  to  $W$  if  $i \in U$  and  $j \in W$ ). Give a randomized  $\frac{1}{4}$  approximation algorithm for this problem.

### Aufgabe 2 (10 Punkte)

Using randomized rounding, show how to obtain a solution for integer multicommodity flow problem such that w.h.p. the number of edges crossing any edge is  $O(\log n / \log \log n)$  times the optimal value  $W^*$ , if  $W^* \geq 1$ .

### Aufgabe 3 (10 Punkte)

Let  $G$  be a complete undirected graph in which all edge lengths are either 1 or 2. Give a  $\frac{4}{3}$  approximation algorithm for TSP in this special class of graphs.